GRG Part III, M 2011

Percolation and related topics II

Exercises will be taken mostly from my book *Probability on Graphs*, published by Cambridge University Press in 2010, and available online at

http://www.statslab.cam.ac.uk/~grg/books/pgs.html

Scripts to be handed in to lecturer (or via pigeon-hole) by **12 noon on Thursday 19 January**. Class to be confirmed, but provisionally timetabled for Thursday 26 January at 3pm in MR13. Please keep an eye on the course webpage for possible changes.

- 1. A critical exponent inequality. Exercise 5.7.
- 2. Russo's formula. Exercise 4.9.
- 3. Using sharp-threshold. Exercise 4.11. This is an example of influence theorems in action.
- 4. Word percolation. Exercise 3.11.
- 5. FKG for Ising model. Exercise 7.3.
- 6. Russo formula for random-cluster model. Exercise 8.1.
- 7. FKG for random-cluster model. Exercise 8.2. The expression 'continuation' is misleading and should be overlooked
- 8. Weak limits as $q \to 0$. Exercise 8.6 (but omit the last sentence).
- 9. Comparison inequalities. Exercise 8.7.
- 10. Random-cluster critical points. Exercise 8.12.
- 11. Profit from the vacation!

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