Percolation and related topics I

Exercises will be taken mostly from my book *Probability on Graphs*, published by Cambridge University Press in 2010, and available online at

http://www.statslab.cam.ac.uk/~grg/books/pgs.html

This set of exercises is extracted from the ends of Chapters 3, 4, and 5.

Handout for 21 October. Scripts to be handed in to lecturer (or via pigeon-hole) by **12 noon on 28 October**. Class to be arranged.

- 1. Subadditive inequalities. Exercises 3.1 and 3.2.
- 2. Bond and site critical probabilities. Exercise 3.3. Do you have an idea for the last part?
- 3. Covering graphs. Exercise 3.4.
- 4. *The problem of runs.* Exercises 3.7 and 3.8. Do not worry overmuch about the fact that you need to work with integer-values. This is 'just noise'.
- 5. Exercise 3.9. This is the open problem that I omitted to mention the other day. You will need to know that $\theta(\frac{1}{2}) = 0$ for bond percolation on the square lattice.
- 6. Exercise 3.10, suggested by a French colleague.
- 7. Positive-correlation for product measures. Exercises 4.2 and 4.3.
- 8. Equivalence of FKG condition and monotonicity. Exercise 4.5.
- 9. A critical-exponent inequality. Exercise 5.1.
- 10. Optional preparation for Cardy's formula. Exercise 5.7.